Mixed Numbers Conversions and Operations

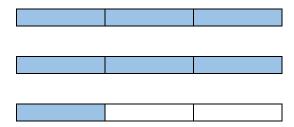
Objective 1: Changing from Mixed Numbers to Improper Fractions & Vice Versa

A fraction is a proper fraction if the numerator is smaller than the denominator.

The numerator in an improper fraction is at least as large as the denominator.

Example: Use the diagram to answer the following:

- a. Write a mixed number to represent the shaded area.
- b. Write a fraction to represent the shaded area.



Change a Mixed Number to an Improper Fraction

- 1. Multiply the whole number by the denominator
- 2. Add the result to the numerator
- 3. Denominator stays the same

Change an Improper Fraction into a Mixed Number

- 1. Divide the denominator into the numerator
- 2. Write your answer as $quotient + \frac{remainder}{divisor}$ (the "+" sign is not written, but understood)

Example: Change $5\frac{2}{7}$ to an improper fraction.

Example: Change $4\frac{3}{5}$ to an improper fraction.

Example: Change $\frac{38}{3}$ to a mixed number.

Example: Change $\frac{45}{7}$ to a mixed number.

Questions

1. Change $4\frac{3}{5}$ to an improper fraction.

2. Change $6\frac{2}{7}$ to an improper fraction.

3. Change $\frac{27}{5}$ to a mixed number.

4. Change $\frac{100}{19}$ to a mixed number.

Objective 2: Multiplying and Dividing Mixed Numbers

Multiplying Mixed Numbers

- 1. Change mixed numbers to improper fractions
- 2. Reduce if possible
- 3. Multiply straight across
- 4. If the answer is an improper fraction change it to a mixed number.

Example: Multiply $\frac{8}{9} \cdot 5\frac{3}{4}$

Example: Multiply $4\frac{1}{2} \cdot 2\frac{2}{3}$

Dividing Mixed Numbers

- 1. Change mixed numbers to improper fractions
- 2. Multiply the first fraction by the reciprocal of the second fraction
- 3. Reduce if possible
- 4. Multiply straight across
- 5. If the answer is an improper fraction change it to a mixed number.

Example: Divide $3\frac{1}{9} \div 2\frac{1}{3}$

Example: Divide $4\frac{2}{3} \div 3$

Questions

1. Multiply
$$\frac{2}{3} \cdot 5\frac{1}{2}$$

2. Multiply
$$3\frac{2}{5} \cdot 3\frac{1}{3}$$

3. Multiply
$$4\frac{4}{5} \cdot 1\frac{5}{6}$$

4. Divide
$$4\frac{2}{5} \div 3\frac{1}{5}$$

5. Divide
$$4\frac{2}{5} \div 8$$

Objective 3: Adding and Subtracting Mixed Numbers

Adding Mixed Numbers

- 1. Add the whole numbers.
- 2. Add the fractions.
- 3. If the fraction is greater than or equal to 1
 - Change into a mixed number.
 - Add to the whole number.

Example: Add
$$4\frac{1}{12} + 2\frac{7}{12}$$

Example: Add
$$9\frac{5}{7} + 2\frac{4}{7}$$

Example: Add
$$5\frac{5}{8} + 2\frac{1}{5}$$

 $\underline{\textbf{Example}} \colon \mathsf{Add} \ \ 3\frac{11}{12} + 1\frac{7}{8}$

Subtracting Mixed Numbers

- 1. Find the LCD for the fractions & make them into LIKE fractions.
- 2. If the first fraction is LARGER than the second fraction
 - Subtract whole numbers
 - Subtract fractions
- 3. If the first fraction is SMALLER than the second fraction
 - Borrow ONE from the whole number
 - Your new numerator is the sum of the numerator & denominator
 - Subtract whole numbers & fractions

Example: Subtract $5-1\frac{3}{8}$

Example: Subtract
$$11\frac{3}{8} - 3\frac{7}{8}$$

Example: Subtract
$$6\frac{1}{10} - 1\frac{8}{15}$$

Example: Subtract
$$12\frac{3}{10} - 4\frac{9}{14}$$

Questions

1. Add
$$12\frac{1}{14} + 3\frac{5}{14}$$

2. Add
$$8\frac{3}{5} + 13\frac{4}{5}$$

3. Add
$$7\frac{7}{9} + 8\frac{5}{6}$$

4. Subtract
$$9-2\frac{3}{5}$$

5. Subtract
$$12\frac{1}{5} - 11\frac{2}{7}$$

Objective 4: Using a Scientific Calculator to do Operations on Mixed Numbers and Fractions



Many Scientific Calculators have a fraction button on them that helps you to easily work with fractions.

To reduce a fraction to lowest terms, input the numerator, then hit the fraction button, followed by the denominator.

Example: Reduce $\frac{6}{8}$ to lowest terms using the calculator.

Example: Add $\frac{1}{2} + \frac{1}{4}$ on the calculator.

Example: Multiply $2\frac{1}{4} \times 5\frac{2}{3}$

Example: Use a calculator to change $4\frac{2}{3}$ into an improper fraction.

Questions

Use a scientific calculator for each of the following problems.

- 1. Reduce $\frac{120}{504}$ to lowest terms.
- 2. Add and simplify: $2\frac{5}{12} \frac{11}{30}$
- 3. Change $\frac{46}{21}$ into a mixed number.

- 4. Change $3\frac{19}{27}$ into an improper fraction.
- 5. Multiply and simplify: $5\frac{4}{7} \times 2\frac{8}{11}$